

The “Goldilocks” Pulse: Mechanistic Constraints on Dose-per-Pulse and Repetition Rate for FLASH Sparing

Why mean dose rate alone does not predict FLASH sparing

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TAKE-HOME MESSAGE

Mean dose rate is a summary metric — not the control variable. FLASH sparing depends on whether oxygen depletion accumulates between pulses.

① High dose-per-pulse drives transient hypoxia

② Short inter-pulse gap limits reoxygenation

③ Intermediate pO_2 sits on steep OER slope

ABSTRACT

We modeled 10 Gy FLASH delivery as equal pulse trains with independently varied pulse number N and repetition rate f using an oxygen-dependent modified LPL framework. Differential sparing was quantified as $\Lambda = \ln(SF_{FLASH}/SF_{CONV})$ for baseline oxygenations of 0.2, 3, and 30 mmHg. The largest pulse-structure sensitivity occurred at 3 mmHg, where high dose-per-pulse and incomplete inter-pulse reoxygenation shift nuclear oxygen along the steep portion of the OER curve. In contrast, very hypoxic and well-oxygenated regimes were comparatively insensitive to pulse structure. These results suggest that mean dose rate is an incomplete descriptor of FLASH biology unless dose-per-pulse, pulse spacing, and oxygenation regime are also specified.

RESULTS: SIMULATION DATA

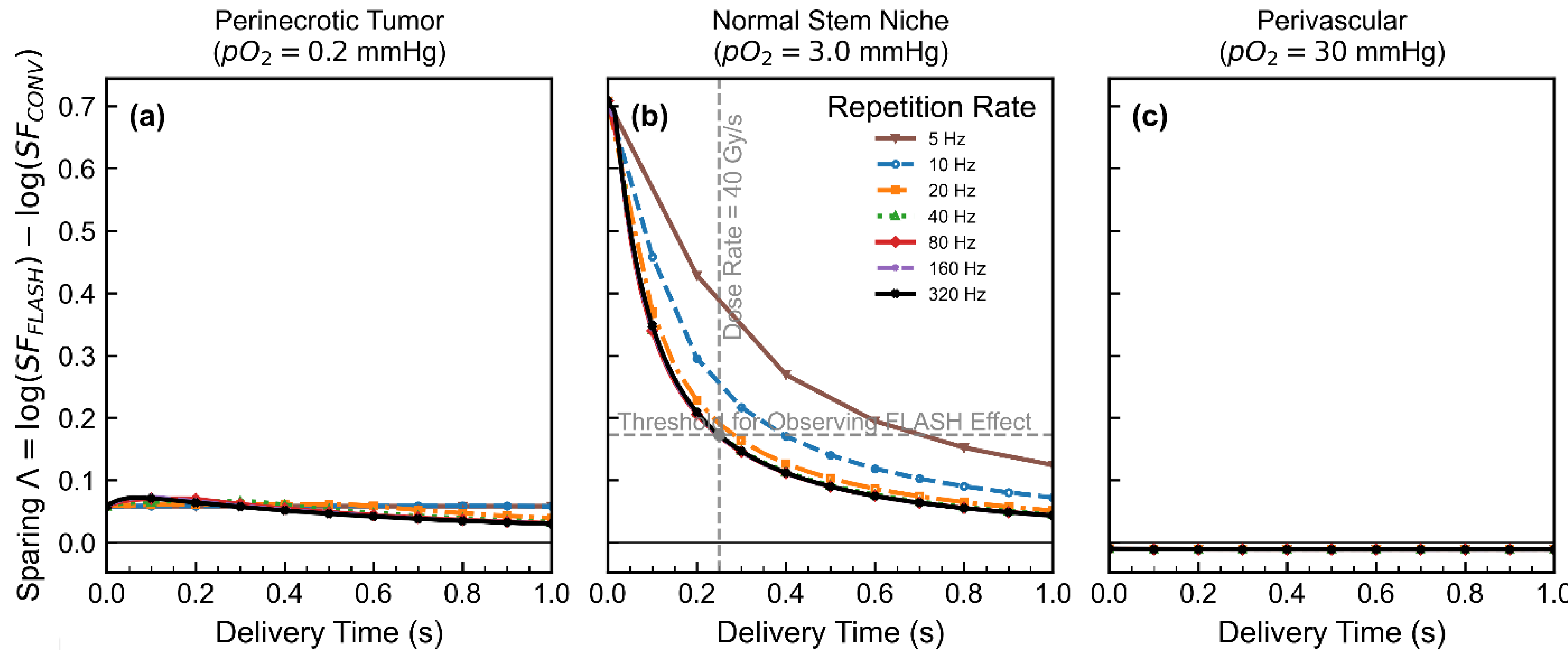


Fig. 2 Differential sparing Λ versus delivery time for 10 Gy. Only the 3-mmHg niche exhibits strong pulse-structure dependence; oxygen extremes are nearly invariant.

Identical MDR can hide different biology because dose-per-pulse and recovery time are independent variables.

Table 2. Pulse-structure comparison for fixed $D = 10$ Gy

Case	N	f (Hz)	d_p (Gy)	Time (s) $T = (N-1)/f$	MDR (Gy/s)	Mechanistic expectation
Few large pulses	5	5	2.00	0.80	12.5	High d_p ; strong transient hypoxia despite modest MDR
MDR benchmark	11	40	0.91	0.25	40.0	Moderate d_p near FLASH threshold
Same MDR, many pulses	81	320	0.12	0.25	40.0	Same MDR but smaller d_p ; less depletion per pulse
Many low-frequency pulses	100	20	0.10	4.95	2.0	Low d_p plus recovery; weak sparing expected

Why only intermediate oxygenation is pulse-sensitive

0.2 mmHg
Already near OER floor
→ little additional sparing from transient depletion

3 mmHg
On steep OER slope
→ **strongest Λ response** to pulse structure

30 mmHg
Near OER plateau
→ depletion insufficient to move biology much

INTRODUCTION

FLASH delivery is often summarized by mean dose rate (MDR), but pulsed beams with identical MDR can differ in dose-per-pulse and inter-pulse recovery. In the modified LPL (m-LPL) framework, radiation creates precursor lesions. Each pulse depletes nuclear oxygen; each gap allows reoxygenation. Question: For fixed total dose, which pulse number N and inter-pulse gap Δt maximize Λ ?

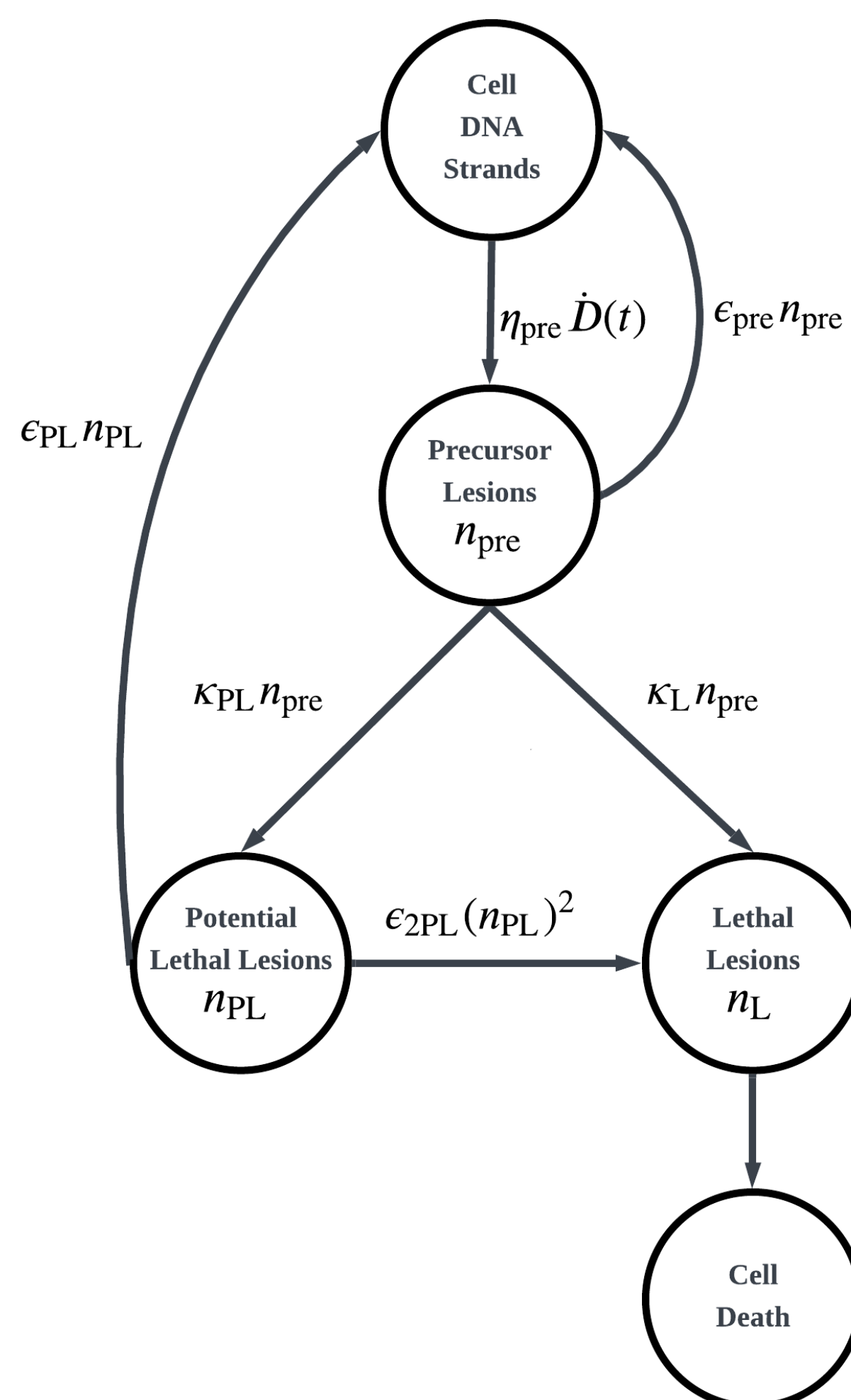


Fig. 3 Coupled oxygen dynamics, repair, and fixation in the modified LPL model.

Biological readout

- Oxygen-dependent modified LPL model
- Per-pulse oxygen depletion and inter-pulse reoxygenation
- Sparing metric: $\Lambda = \ln(SF_{FLASH}/SF_{CONV})$

Table 1. Key simulation parameters

Group	Parameter	Symbol	Value
Fix.	Precursor formation	η_{pre}	2000 Gy ⁻¹
Fix.	Precursor decay	ϵ_{pre}	50 s ⁻¹
Fix.	L / PL fixation	η_L η_{PL}	0.137/Gy 0.6/Gy
O ₂	Radiolytic yield	G	0.42 mmHg/Gy
O ₂	Reoxygenation	k_{reox}	20 s ⁻¹
O ₂	Michaelis const.	K_g	0.21 mmHg
OER	max/min	—	3.0 / 1.0
OER	Sensitivity	$\sim K_m$	~ 3.0 mmHg

Recommended beam reporting:

D , MDR, N , d_p , f , inter-pulse gap Δt , total delivery time, and target oxygenation regime. This avoids hiding biologically important pulse-structure differences inside MDR.

METHODS AND MATERIALS

Simulation design

- Total dose fixed: $D = 10$ Gy
- Equal pulse trains: $d_p = D/N$
- Pulse number: $N = 1 - 320$
- Repetition rate: $f = 5 - 320$ Hz
- Inter-pulse gap: $\Delta t = 1/f$
- Oxygen regimes: 0.2, 3, 30 mmHg

Visual timeline: pulse number changes dose-per-pulse

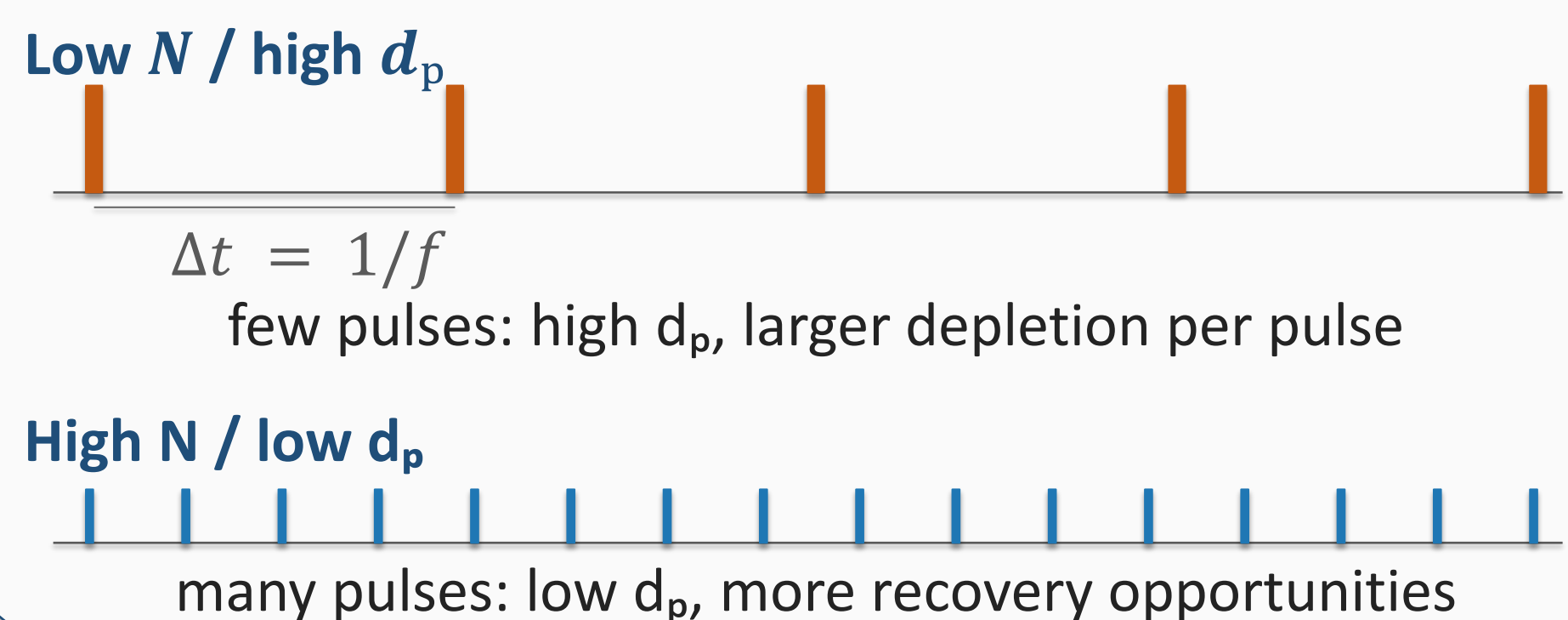


Fig. 1 Fixed D split into fewer pulses gives higher d_p ; larger gaps allow pO_2 recovery.

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DISCUSSION

The simulation supports a mechanistic distinction between average dose rate and biologically effective pulse structure. At fixed total dose, N controls dose-per-pulse and Δt controls inter-pulse recovery.

The normal niche shows the largest Λ because its baseline oxygenation lies near the steep portion of the OER curve. Large pulses can push nuclear oxygen into a transiently radioresistant state.

Table 2 highlights the translational issue: two beams may share the same MDR but differ strongly in d_p . Sparing is controlled by the balance between depletion amplitude per pulse and recovery between pulses.

CONCLUSIONS

Design rules from the model

- Oxygen window matters: FLASH sparing is strongest near the steep OER region, not at oxygen extremes.
- Dose-per-pulse matters: At fixed D , smaller N increases d_p and transient oxygen depletion.
- Recovery time matters: Short Δt preserves depletion; long Δt allows reoxygenation.
- MDR is conditional: Mean dose rate becomes predictive only when pulse spacing is short relative to local reoxygenation.
- Report pulse structure: D , MDR, N , d_p , f , Δt , total delivery time, and oxygenation regime should be reported together.

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